

Separation Logic, Compositional Symbolic Execution and the Gillian Platform

Philippa Gardner
Imperial College London

Challenge: to develop techniques and tools for verification and true bug detection that scale.

Link: <https://gillianplatform.github.io/labs/standv26/>



Lecture 1

Separation Logic and the Gillian Platform

Scalable Software Verification

Some program-analysis techniques based on first-order logic:

- verification based on Hoare logic: e.g. Frama-C;
- symbolic execution: e.g. CBMC.

These techniques are not compositional with respect to the machine state, and **do not scale**.

Some program-analysis techniques, compositional with respect to the machine state:

- separation logics, originally O'Hearn and Reynolds: e.g. the concurrent higher-order Iris framework.
- compositional symbolic execution inspired by separation logics: e.g. the compositional verification tools and platforms Verifast, Viper, Gillian, CN; the true platforms for true bug detection Infer-Pulse, Gillian.

These techniques **do scale**.

The CSE and Gillian Team: Past and Current Members



Philippa Gardner



Diego Cupello



Andreas Lööw



Simon Park



Sacha-Élie Ayoun



Caroline Cronjäger



Petar Maksimović



José Fragoso Santos



Nat Karmios



Daniele Nantes



Opale Sjöstedt



Shiva Tamil Kumaran

Traditional Hoare Logic

Traditional Hoare Triples

This reasoning works with the **whole** memory, using conjunction and the conjunction rule to describe different properties of the memory.

$$\vdash \{ \text{List}(x) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \}$$

$$\not\vdash \{ \text{List}(x) \wedge \text{List}(y) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \wedge \text{List}(y) \}$$

Traditional Hoare Logic

Traditional Hoare Triples

This reasoning works with the **whole** memory, using conjunction and the conjunction rule to describe different properties of the memory.

$$\vdash \{ \text{List}(x) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \}$$

$$\not\vdash \{ \text{List}(x) \wedge \text{List}(y) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \wedge \text{List}(y) \}$$

$$\vdash \{ \text{List}(x) \wedge \text{List}(y) \wedge \text{NReach}(x, y) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \wedge \text{List}(y) \}$$

$$\vdash \{ \text{List}(x) \wedge \text{List}(y) \wedge \text{List}(z) \wedge \text{NReach}(x, y) \wedge \text{NReach}(y, z) \wedge \text{NReach}(z, y) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \wedge \text{List}(y) \wedge \text{List}(z) \}$$

This reasoning does not scale.

Separation Logic: a Modern Hoare Logic

Local Hoare Triples

This reasoning works with **partial** memory.

$$\vdash \{ \text{list}(x) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \}$$

It uses **separating conjunction** and **frame rule** to disjointly extend the memory.

$$\frac{\vdash \{P\} C \{Q\} \quad \text{side-condition}}{\vdash \{P \star R\} C \{Q \star R\}} \text{frame}$$

Separation Logic: a Modern Hoare Logic

Local Hoare Triples

This reasoning works with **partial** memory.

$$\vdash \{ \text{list}(x) \} \text{LDispose}(x) \{ \text{ret} = \text{null} \}$$

$$\vdash \{ \text{list}(x) * \text{list}(y) \} \text{LDispose}(x) \{ \text{ret} = \text{null} * \text{list}(y) \}$$

$$\vdash \{ \text{list}(x) * \text{list}(y) * \text{list}(z) \} \text{LDispose}(x) \{ \text{ret} = \text{null} * \text{list}(y) * \text{list}(z) \}$$

This reasoning does scale.

A Simple While Language

Expressions

Boolean values $b \in \text{Bool} \stackrel{\text{def}}{=} \{\text{true}, \text{false}\}$

Values $v \in \text{Val} \supseteq \mathbb{N} \cup \text{Bool} \cup \{\text{null}\}$

Program Variables $x \in \text{Var}$

Simple Expressions $E \in \text{Exp} ::= v \mid x \mid E + E \mid E - E \mid E \times E \mid E / E$
 $E = E \mid E > E \mid E \wedge E \mid \neg E \mid \dots$

Program State

Variable Store $s \in \text{Store} \stackrel{\text{def}}{=} \text{Var} \rightarrow_{\text{fin}} \text{Val}$

Linear Heap $h \in \text{Heap} \stackrel{\text{def}}{=} \mathbb{N} \rightarrow_{\text{fin}} \text{Val}$

State $\sigma \in \text{State} \stackrel{\text{def}}{=} \text{Store} \times \text{Heap}$

Notation

$\emptyset$ denotes the empty store and $s[x \mapsto v]$ denotes the store with x updated with v .

$\emptyset$ denotes the empty heap and $h_1 \uplus h_2$ denotes the disjoint union of heaps.

Expression Evaluation

$\mathcal{E}[[E]]_s \in \text{Val}$ denotes the value of expression E with respect to the variable store s .

When $\mathcal{E}[[E]]_s \in \text{Bool}$, we say that E is a **Boolean expression**.

Commands

Commands $C ::= x := E \mid x := [E] \mid [E] := E \mid x := \text{new}(E) \mid \text{dispose}(E) \mid x := f(\vec{E}) \mid \text{skip} \mid C; C \mid \text{if } (E) C \text{ else } C \mid \text{while } (E) C$

$[E]$ denotes the value stored at the heap cell with address given by the value of expression E .

Function definition context, γ , maps function identifiers to their implementations:

$$\gamma(f) = (\vec{x}, C, E) \text{ where } \text{pv}(E) \subseteq \{\vec{x}\} \cup \text{pv}(C).$$

We tend to write $f(\vec{x})\{C; \text{return } E\} \in \gamma$ for $\gamma(f) = (\vec{x}, C, E)$.

Operational Semantics $(s, h), C \Downarrow_{\gamma} (s', h')$

Assertion Language

The **assertion language** for separation logic provides **assertions** (formulae) for describing the pre- and post-conditions for the Hoare triples.

Logical Expressions and Logical State

Logical Values $a, a_1, \dots \in \text{LVal} \quad \supseteq \text{Val}$

Logical Variables $x, y, \dots \in \text{LVar}$

Logical Expressions $E \in \text{LExp} ::= a \mid \mathbf{x} \mid x \mid E + E \mid E - E \mid E \times E \mid E / E \mid$
 $E = E \mid E > E \mid E \wedge E \mid \neg E \mid \dots, \text{ for } \mathbf{x} \in \text{PVar}$

Logical Environment $e \in \text{LEnv} \stackrel{\text{def}}{=} \text{LVar} \rightarrow_{\text{fin}} \text{LVal}$

Logical State $(e, s, h) \in \text{LState} \stackrel{\text{def}}{=} \text{LEnv} \times \text{Store} \times \text{Heap}$

Logical expression evaluation

$\mathcal{E}[E]_{e,s} \in \text{Val}$ describes the value of logical expression E with respect to logical store e and variable store s .

Assertions

The set of **assertions**, Assert , is defined by the grammar:

$P \in \text{Assert} ::=$	$P \wedge P \mid P \Rightarrow P \mid \text{True} \mid \text{False}$	classical connectives
	$\mid E = E \mid E > E \mid E \in X \mid \dots$	Boolean assertions
	$\mid \exists x. P$	existential quantification
	$\mid P \star P \mid \text{emp}$	separating connectives
	$\mid E \mapsto E$	linear heap cell assertion
	$\mid \text{pred}(\vec{E})$	predicate assertion

where $X \subseteq \text{LVal}$ and $x \in \text{LVar}$.

Predicate definition: $\text{pred}(\vec{x}) \stackrel{\text{def}}{=} P$, where the free logical variables of P are in $\{\vec{x}\}$.

Satisfiability Relation

The logical state (e, s, h) **satisfies** P , written $e, s, h \models P$, is defined by:

$e, s, h \models P_1 \wedge P_2$	$\iff$	$e, s, h \models P_1 \wedge e, s, h \models P_2$
$e, s, h \models P_1 \Rightarrow P_2$	$\iff$	$e, s, h \models P_1 \implies e, s, h \models P_2$
$e, s, h \models \mathbf{True}$	$\iff$	always
$e, s, h \models \mathbf{False}$	$\iff$	never
$e, s, h \models E_1 = E_2$	$\iff$	$(\mathcal{E}\llbracket E_1 = E_2 \rrbracket_{e,s} = \mathbf{true}) \wedge h = \emptyset$
$e, s, h \models E_1 > E_2$	$\iff$	$(\mathcal{E}\llbracket E_1 > E_2 \rrbracket_{e,s} = \mathbf{true}) \wedge h = \emptyset$
$e, s, h \models E \in X$	$\iff$	$(\mathcal{E}\llbracket E \in X \rrbracket_{e,s} = \mathbf{true}) \wedge h = \emptyset$
$e, s, h \models \exists x. P$	$\iff$	$\exists v \in \mathbf{Val}. e[x \mapsto v], s, h \models P$
$e, s, h \models P_1 \star P_2$	$\iff$	$\exists h_1, h_2 \in \mathbf{Heap}. h = h_1 \uplus h_2 \wedge e, s, h_1 \models P_1 \wedge e, s, h_2 \models P_2$
$e, s, h \models \mathbf{emp}$	$\iff$	$h = \emptyset$
$e, s, h \models E_1 \mapsto E_2$	$\iff$	$h = \{\mathcal{E}\llbracket E_1 \rrbracket_{e,s} \mapsto \mathcal{E}\llbracket E_2 \rrbracket_{e,s}\}$
$e, s, h \models \mathbf{pred}(\vec{E})$	$\iff$	$\mathbf{pred}(\vec{x}) \stackrel{\text{def}}{=} P \wedge e, s, h \models P[\vec{E}/\vec{x}]$

We write $\llbracket P \rrbracket_{e,s} \stackrel{\text{def}}{=} \{h : e, s, h \models P\}$.

Exercise

State whether each assertion is satisfiable or unsatisfiable; when satisfiable, describe the heaps that satisfy the assertion.

① $10 \mapsto 1 \star 10 \mapsto 1$

② $10 \mapsto 1 \star 10 \mapsto 2$

③ $10 \mapsto 1 \wedge 11 \mapsto 1$

Additional questions and all answers given on our webpage.

Some Properties

An assertion P is **valid**, written $\models P$, if $e, s, h \models P$ for all e, s and h .

Some properties of $\star$: commutativity, associativity, unit emp, scope extrusion of the existential and some distributivity:

$$\begin{aligned}\models (P_1 \wedge P_2) \star Q &\Rightarrow (P_1 \star Q) \wedge (P_2 \star Q) \\ \models (P_1 \vee P_2) \star Q &\Leftrightarrow (P_1 \star Q) \vee (P_2 \star Q)\end{aligned}$$

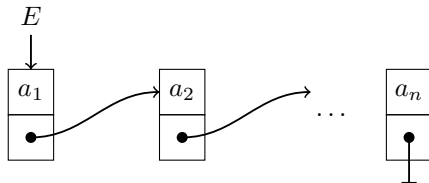
Some properties of the cell assertion:

$$\begin{aligned}\models E_1 \mapsto E_2 &\Rightarrow E_1 \in \mathbb{N} \wedge E_2 \in \text{Val} \\ \models E_1 \mapsto E_2 \star E_3 \mapsto E_4 &\Rightarrow E_1 \neq E_3 \\ \models E_1 \mapsto E_2 \wedge E_3 \mapsto E_4 &\Rightarrow E_1 = E_3 \wedge E_2 = E_4\end{aligned}$$

Derived Assertions and Predicate Definitions

$$\begin{aligned} E \mapsto - &\stackrel{\text{def}}{=} \exists x. E \mapsto x, \text{ for } x \text{ not free in } E \\ E \mapsto E_1, E_2 &\stackrel{\text{def}}{=} (E \mapsto E_1) \star (E + 1 \mapsto E_2) \\ \text{list}(x, \alpha) &\stackrel{\text{def}}{=} (x = \text{null} \star \alpha = []) \vee (\exists a, l_1, y. x \mapsto a, y \star \text{list}(y, \alpha_1) \star \alpha = a:\alpha_1) \end{aligned}$$

Predicate $\text{list}(E, \alpha)$ is satisfied by a singly-linked list that has the shape



where $\alpha = [a_1, a_2, \dots, a_n]$.

List Predicate with Values: Properties

Exercise

- $\models \text{list}(E, []) \Rightarrow$ What does that tell us about E ?
- $\models \text{list}(E, a:\alpha) \Rightarrow$ What does that tell us about E ?
- $\models \text{list}(\text{null}, \alpha) \Rightarrow$ What does that tell us about α ?
- $\models E_1 \mapsto E_2 \star \text{list}(E_3, \alpha) \star E_3 \neq \text{null} \Rightarrow$ What is the relationship between E_1 and E_3 ?

Separation Logic

Hoare Triples

A **Hoare triple**, $\{P\}C\{Q\}$, is a relation between two assertions P and Q and command C where P is called the **pre-condition** and Q the **post-condition**.

A Hoare triple of a command C is **valid**, written

$$\models \{P\}C\{Q\}$$

if and only if, starting in any logical state in which the assertion P holds, no execution of the simple command C aborts and, for any execution of C that terminates, the assertion Q holds in the final logical state.

The proof rules of separation logic provide a way of discovering valide Hoare triples, written $\vdash \{P\}C\{Q\}$. These rules are given on our webpage for OPLSS'26.

Soundness $\vdash \{P\}C\{Q\} \Rightarrow \models \{P\}C\{Q\}$

LLen(x): List Length

```
LLen(x) {  
  if (x = null) {  
    n := 0  
  } else {  
    t := [x + 1];  
    n := LLen(t);  
    n := n + 1  
  };  
  return n  
}
```

```
LLen(x) {  
  y := x;  
  n := 0;  
  while (y ≠ null) {  
    y := [y + 1];  
    n := n + 1  
  };  
  return n  
}
```

where $[x + 1]$ denotes the contents of the storage at the address given by expression $x + 1$.

LLen(x) Proof Sketch: function entry and base case

```
⊢ {x = x ★ list(x, α)}
LLen(x) {
  // Initialise the local variables and ensure the Boolean condition is evaluable.
  {x = x ★ list(x, α) ★ n, t = null}
  {x = x ★ list(x, α) ★ n, t = null ★ (x = null) ∈ Bool}
  if (x = null) {
    {x = x ★ list(x, α) ★ n, t, x = null}
    // As x = null, unfolding the list predicate yields the base case.
    {x = x ★ (x = null ★ α = []) ★ n, t = null}
    n := 0
    {x = x ★ (x = null ★ α = []) ★ t = null ★ n = 0}
    // Forget x and t as no longer used, connect n to α, and fold back list predicate.
    {(x = null ★ α = []) ★ n = |α|}
    {list(x, α) ★ n = |α|}
  } else {
```

LLen(x) Proof Sketch: recursive case

```
} else {  
  { $x = x \star \text{list}(x, \alpha) \star n, t = \text{null} \star x \neq \text{null}$ }  
  // Unfold list predicate to recursive case, identify the resource needed  
  { $\exists v, \beta, y. x \mapsto v, y \star \alpha = v:\beta \star \text{list}(y, \beta) \star n, t = \text{null}$ }  
  exists, frame + cons | { $x \mapsto v, y \star \text{list}(y, \beta) \star n, t = \text{null}$ }  
    t := [x + 1];  
    // Use the fcall rule to consume precondition and produce postcondition.  
    { $x \mapsto v, y \star \text{list}(y, \beta) \star n = \text{null} \star t = y$ }  
    n := llen(t);  
    { $x \mapsto v, y \star \text{list}(y, \beta) \star n = |\beta|$ }  
    n := n + 1  
    { $x \mapsto v, y \star \text{list}(y, \beta) \star n = |\beta| + 1$ }  
  // frame back assertions, add exists and fold back list predicate.  
  { $\exists v, \beta, y. x \mapsto v, y \star \alpha = v:\beta \star \text{list}(y, \beta) \star n = |\beta| + 1$ }  
  { $\text{list}(x, \alpha) \star n = |\alpha|$ }  
}
```

LLen(x) Proof Sketch: end of conditional statement

```
⊢ {x = x ★ list(x, α)}  
LLen(x) {  
  {x = x ★ list(x, α) ★ n, t = null}  
  {x = x ★ list(x, α) ★ n, t = null ★ (x = null) ∈ Bool}  
  if (x = null) {  
    ...  
    {list(x, α) ★ n = |α|}  
  } else {  
    ...  
    {list(x, α) ★ n = |α|}  
  }  
  // As the post-condition of both the if and else bodies are the same,  
  // we infer the post-condition of the conditional statement.  
  {list(x, α) ★ n = |α|}  
  return n  
}  
{list(x, α) ★ ret = |α|}
```

LLen(x): List Length

```
LLen(x) {  
  if (x = null) {  
    n := 0  
  } else {  
    t := [x + 1];  
    n := LLen(t);  
    n := n + 1  
  };  
  return n  
}
```

```
LLen(x) {  
  y := x;  
  n := 0;  
  while (y ≠ null) {  
    y := [y + 1];  
    n := n + 1  
  };  
  return n  
}
```

where $[x + 1]$ denotes the contents of the storage at the address given by expression $x + 1$.

Iterative List-length Algorithm

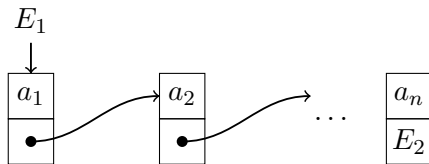
Consider an iterative list-length algorithm where $|\alpha|$ is the length of the list α

```
⊢ { $x = x \star \text{list}(x, \alpha)$ }  
  LLen( $x$ ) {  
    { $x = x \star \text{list}(x, \alpha) \star y, n = \text{null}$ }  
     $y := x; n := 0;$   
    { $\exists \alpha_1, \alpha_2. ??? \star \text{list}(y, \alpha_2) \star \alpha = \alpha_1 \cdot \alpha_2 \star n = |\alpha_1|$ }  
    while ( $y \neq \text{null}$ ) {  
       $y := [y + 1];$   
       $n := n + 1;$   
    }  
    { $\text{list}(x, \alpha) \star n = |\alpha|$ }  
    return  $n$ ;  
  }  
  { $\text{list}(x, \alpha) \star \text{ret} = |\alpha|$ }
```

List-segment Predicate

$$\text{lseg}(x, z, l) \stackrel{\text{def}}{=} (x = z \star l = []) \vee (\exists a, y, l_1. x \mapsto a, y \star \text{lseg}(y, z, l_1) \star l = a:l_1)$$

Predicate $\text{lseg}(E_1, E_2, \alpha)$ is satisfied by an incomplete singly-linked list that has the shape



List-segment Predicate: Properties

The following properties hold for the list-segment predicate:

$$\models \text{list}(E, \alpha) \Leftrightarrow \text{lseg}(E, \text{null}, \alpha)$$

$$\models \text{lseg}(E_1, E_2, \alpha) \star \text{lseg}(E_2, E_3, \beta) \Rightarrow \text{lseg}(E_1, E_3, \alpha \cdot \beta)$$

$$\models \text{lseg}(E_1, E_2, \alpha) \star \text{list}(E_2, \beta) \Rightarrow \text{list}(E_1, \alpha \cdot \beta)$$

$$\models \text{lseg}(E_1, E_2, \alpha) \star E_2 \mapsto a, E_3 \Rightarrow \text{lseg}(E_1, E_3, \alpha \cdot [a])$$

where $[a]$ denotes the single-element list containing a .

LLen(x) Proof Sketch: function entry and loop invariant

```
⊢ {x = x * list(x, α)}
  LLen(x) {
    {x = x * list(x, α) * y, n = null}
    y := x;
    {x = x * list(x, α) * y = x * n = null}
    // Forget x as it is no longer used
    {list(x, α) * y = x * n = null}
    n := 0;
    {list(x, α) * y = x * n = 0}
    // Set up the loop invariant: the traversed part (initially, nothing) is a list segment from x to y,
    // the untraversed part (initially, everything) is a list at y, the contents of the two parts (initially, [] and α)
    // form the full list contents α, and n is counting the length of the traversed part
    {∃α₁, α₂. lseg(x, y, α₁) * list(y, α₂) * α = α₁ · α₂ * n = |α₁| * (y ≠ null ∈ Bool)}
    while (y ≠ null) {
      // Loop entry: invariant and loop condition
      {∃α₁, α₂. lseg(x, y, α₁) * list(y, α₂) * α = α₁ · α₂ * n = |α₁| ∧ y ≠ null}
      ...
    }
  }
```

LLen(x) Proof Sketch: proving the loop body

```
while (y ≠ null) {  
  { $\exists \alpha_1, \alpha_2. \text{lseg}(x, y, \alpha_1) \star \text{list}(y, \alpha_2) \star \alpha = \alpha_1 \cdot \alpha_2 \star \mathbf{n} = |\alpha_1| \wedge y \neq \text{null}$ }  
  // Unfold the shaded predicate to gain access to [y + 1]  
  { $\exists \alpha_1, \alpha_2, \alpha_3, a, z. \text{lseg}(x, y, \alpha_1) \star y \mapsto a, z \star \text{list}(z, \alpha_3) \star \alpha_2 = a:\alpha_3 \star \alpha = \alpha_1 \cdot \alpha_2 \star \mathbf{n} = |\alpha_1|$ }  
  // Record previous value of y as loop body changes y  
  { $\exists \alpha_1, \alpha_3, y, a, z. y = y \star \text{lseg}(x, y, \alpha_1) \star y \mapsto a, z \star \text{list}(z, \alpha_3) \star \alpha = \alpha_1 \cdot (a:\alpha_3) \star \mathbf{n} = |\alpha_1|$ }  
  // Isolate the resource of the loop  
  exists, frame, cons |  
    { $y = y \star y \mapsto a, z \star \mathbf{n} = |\alpha_1|$ }  
    y := [y + 1];  
    { $y = z \star y \mapsto a, z \star \mathbf{n} = |\alpha_1|$ }  
    n := n + 1;  
    { $y = z \star y \mapsto a, z \star \mathbf{n} = |\alpha_1| + 1$ }  
  // Bring back the existentials and frame  
  { $\exists \alpha_1, \alpha_3, y, a, z. y = z \star y \mapsto a, z \star \mathbf{n} = |\alpha_1| + 1 \star \text{lseg}(x, y, \alpha_1) \star \text{list}(z, \alpha_3) \star \alpha = \alpha_1 \cdot (a:\alpha_3)$ }
```

LLen(x) Proof Sketch: exiting the loop and function exit

```
// Bring back the existentials and frame
{ $\exists \alpha_1, \alpha_3, y, a, z. y = z \star y \mapsto a, z \star n = |\alpha_1| + 1 \star \text{lseg}(x, y, \alpha_1) \star \text{list}(z, \alpha_3) \star \alpha = \alpha_1 \cdot (a:\alpha_3)$ }
// Re-establish the loop invariant
{ $\exists \alpha_1, \alpha_3, y, a. \text{lseg}(x, y, \alpha_1) \star y \mapsto a, y \star \text{list}(y, \alpha_3) \star \alpha = \alpha_1 \cdot (a:\alpha_3) \star n = |\alpha_1| + 1$ }
// Apply lemma: (shaded) list segment  $\star$  node at end  $\rightarrow$  extended list segment
{ $\exists \alpha_1, \alpha_3, y, a. \text{lseg}(x, y, \alpha_1 \cdot [a]) \star \text{list}(y, \alpha_3) \star \alpha = (\alpha_1 \cdot [a]) \cdot \alpha_3 \star n = |\alpha_1 \cdot [a]|$ }
{ $\exists \alpha_1, \alpha_2. \text{lseg}(x, y, \alpha_1) \star \text{list}(y, \alpha_2) \star \alpha = \alpha_1 \cdot \alpha_2 \star n = |\alpha_1| \star (y \neq \text{null} \in \text{Bool})$ }
}
{ $(\exists \alpha_1, \alpha_2. \text{lseg}(x, y, \alpha_1) \star \text{list}(y, \alpha_2) \star \alpha = \alpha_1 \cdot \alpha_2 \star n = |\alpha_1|) \wedge y = \text{null}$ }
{ $\exists \alpha_1, \alpha_2. \text{lseg}(x, \text{null}, \alpha_1) \star \text{list}(\text{null}, \alpha_2) \star \alpha = \alpha_1 \cdot \alpha_2 \star n = |\alpha_1|$ }
// Apply lemma: (shaded) list segment ending with null is a list
{ $\exists \alpha_1, \alpha_2. \text{list}(x, \alpha_1) \star \alpha_2 = [] \star \alpha = \alpha_1 \cdot \alpha_2 \star n = |\alpha_1|$ }
{ $\text{list}(x, \alpha) \star n = |\alpha|$ }
return n;
}
// Assign return value
{ $\text{list}(x, \alpha) \star n = |\alpha| \star \text{ret} = n$ }
{ $\text{list}(x, \alpha) \star \text{ret} = |\alpha|$ }
```

Exercise: List Concatenation

```
list_concat(x, y) {  
    if (x = null) {  
        x := y  
    } else {  
        t := x;  
        n := [x + 1];  
        while (n ≠ null) {  
            t := n;  
            n := [n + 1]  
        };  
        [t + 1] := y  
    };  
    return x  
};
```

A Gillian Taster

Link: <https://youtu.be/5TTBX4ecZkk>

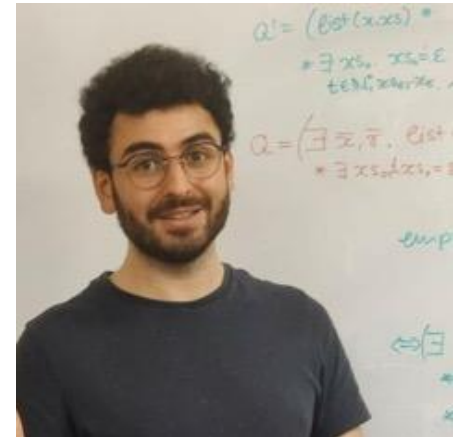
The Gillian Platform

Semi-automatic Verification & Automatic True Bug Detection

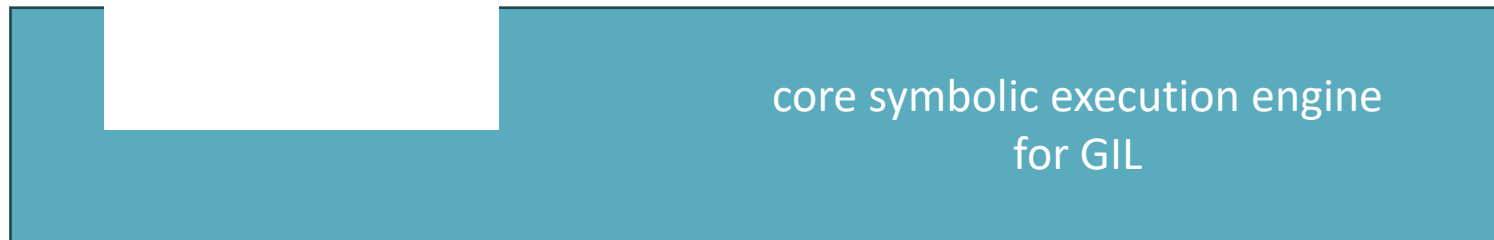
Gillian Platform: PLDI'20, CAV'21

A general platform for the development of compositional analysis tools with strong mathematical foundations:

- Parametric on the partial symbolic state
- Gillian-specific match/consume and produce algorithms satisfy the properties of the algebraic interface
- Gillian-JavaScript and Gillian-C and Gillian-Rust [PLDI'25] tool instantiations
- Applications to semi-automatic verification and true bug detection for real-world code:
e.g., verification of the JS implementation (200 loc) and C implementation (900 loc) of critical AWS encryption SDK code



Gillian: Parametric Symbolic Execution



Gillian: Parametric Symbolic Execution

quite literally speaking

- *Interpreter with SMT queries sent right when needed*
- *Its own incremental SMT solver with a Z3 fallback*



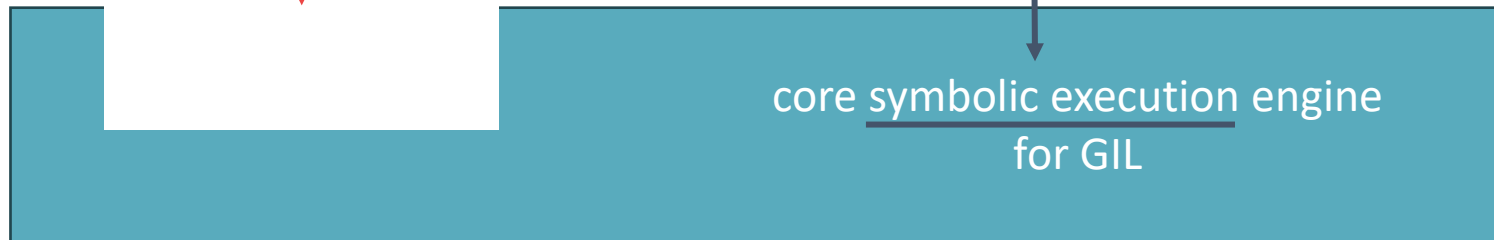
core symbolic execution engine
for GIL

Gillian: Parametric Symbolic Execution

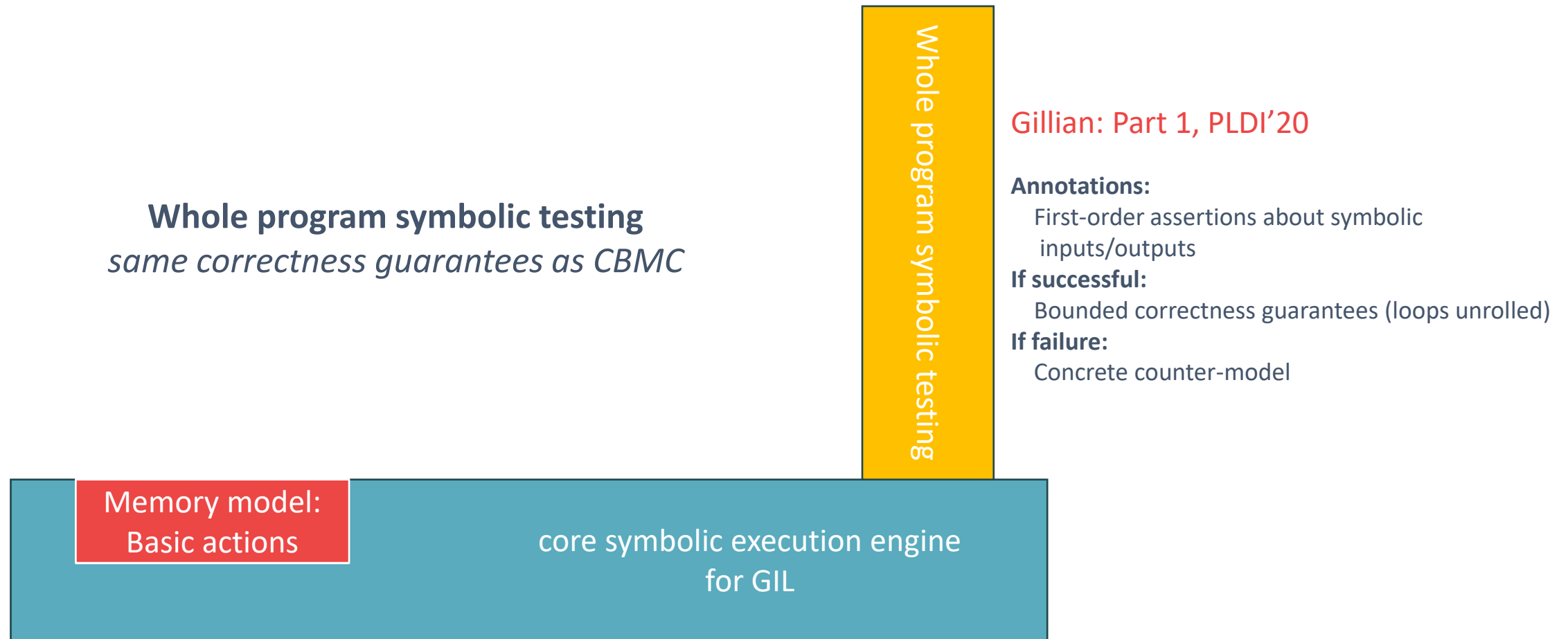
Semantic hole: memory operations
e.g. load, store, pointer validity checks in C,
prototype access in JS...

quite literally speaking

- *Interpreter with SMT queries sent right when needed*
- *Its own incremental SMT solver with a Z3 fallback*

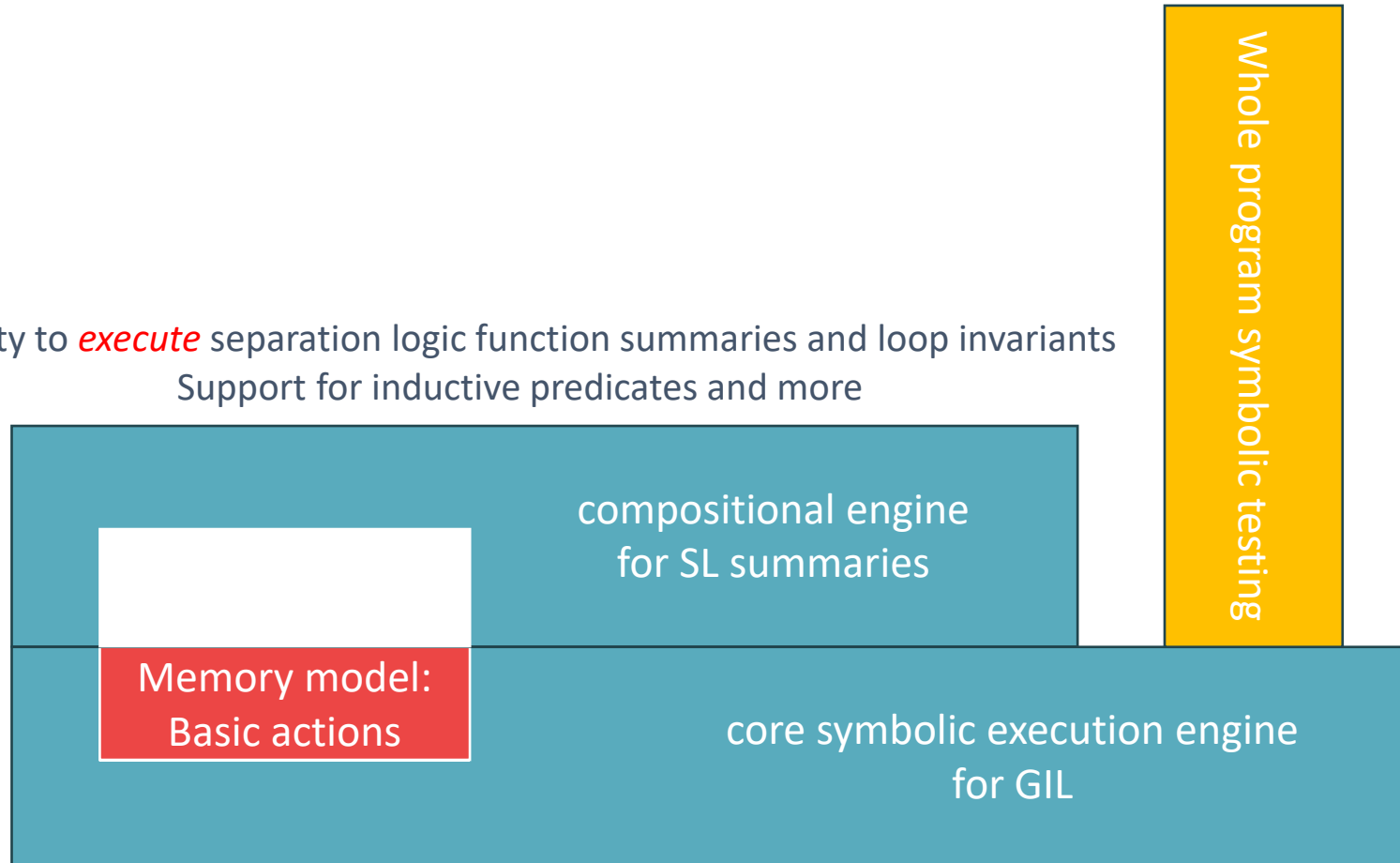


Gillian: Parametric Symbolic Execution



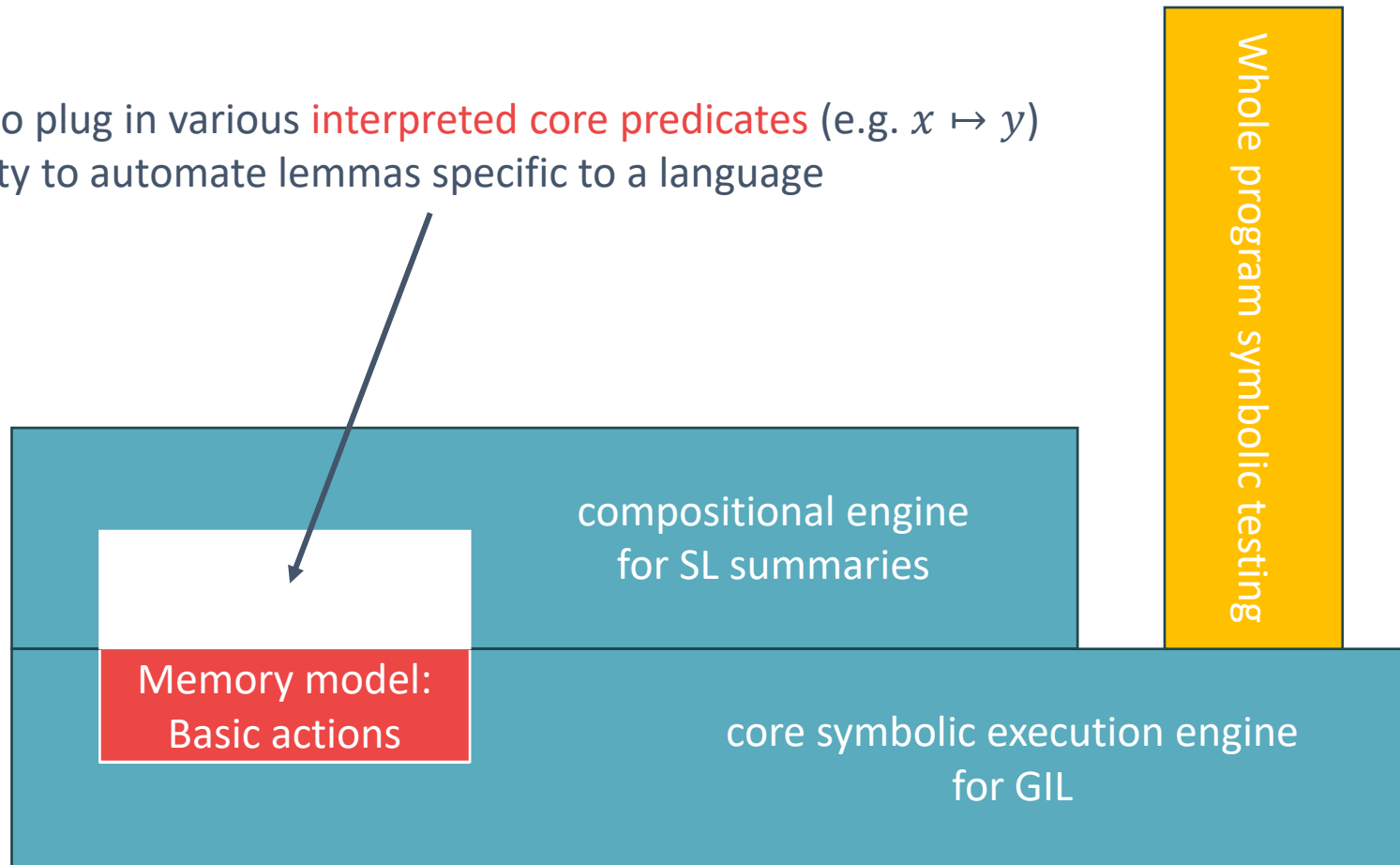
Gillian: Compositional Parametric Symbolic Execution

Ability to *execute* separation logic function summaries and loop invariants
Support for inductive predicates and more



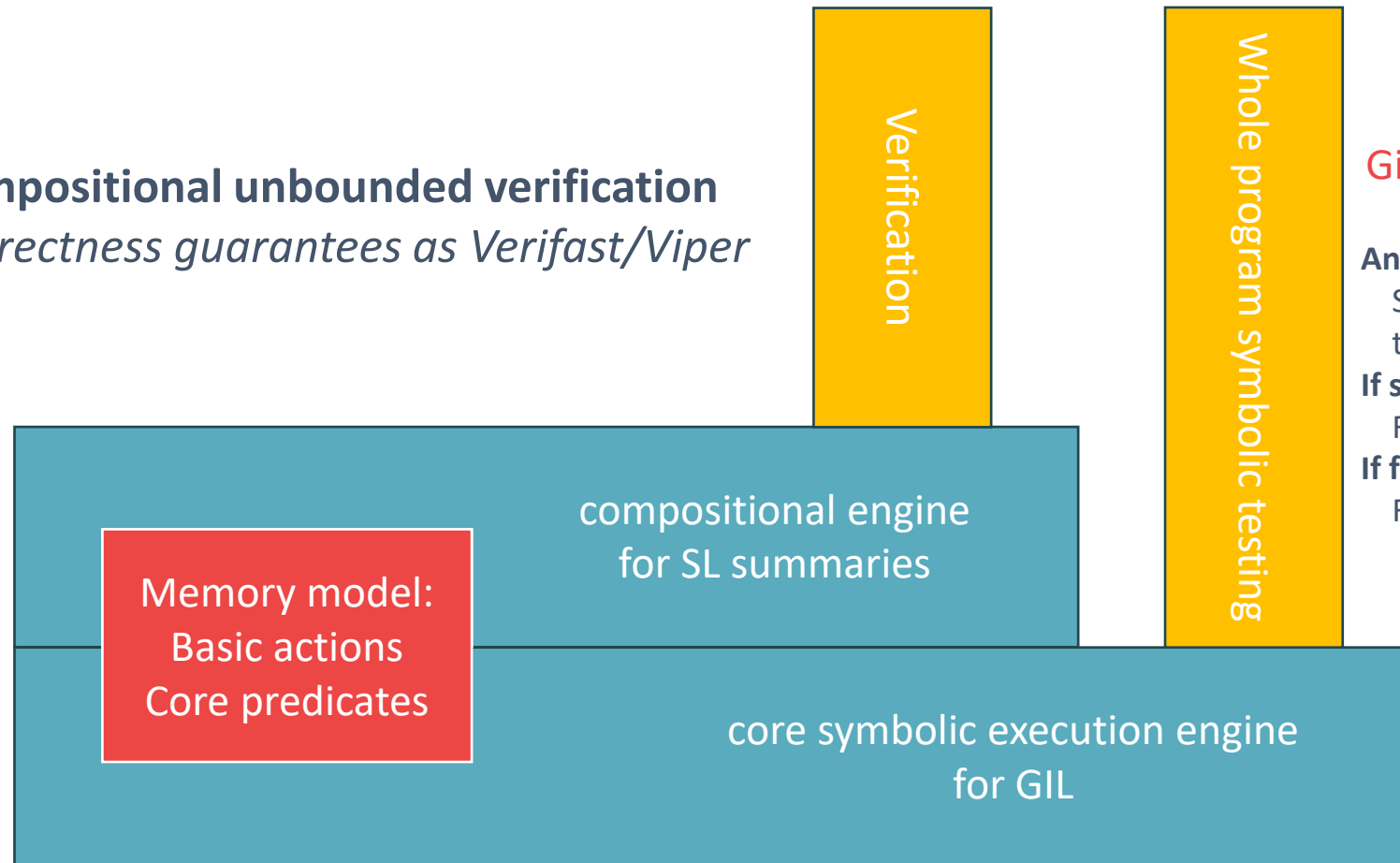
Gillian: **Compositional** Parametric Symbolic Execution

Ability to plug in various **interpreted core predicates** (e.g. $x \mapsto y$)
=> Ability to automate lemmas specific to a language



Gillian: Compositional Parametric Symbolic Execution

Full compositional unbounded verification
same correctness guarantees as Verifast/Viper



Gillian: Part 2, CAV'21

Annotations:

Separation logic specs, invariants, lemmas, tactics...

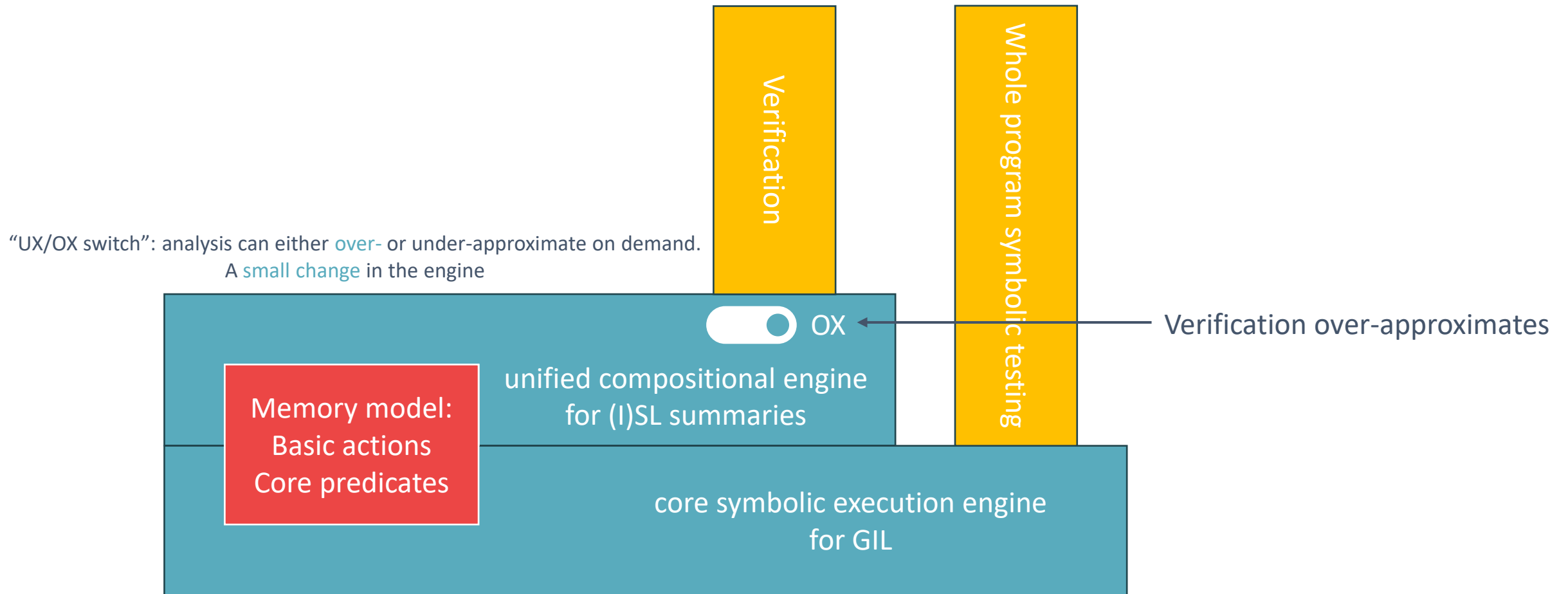
If successful:

Functional correctness

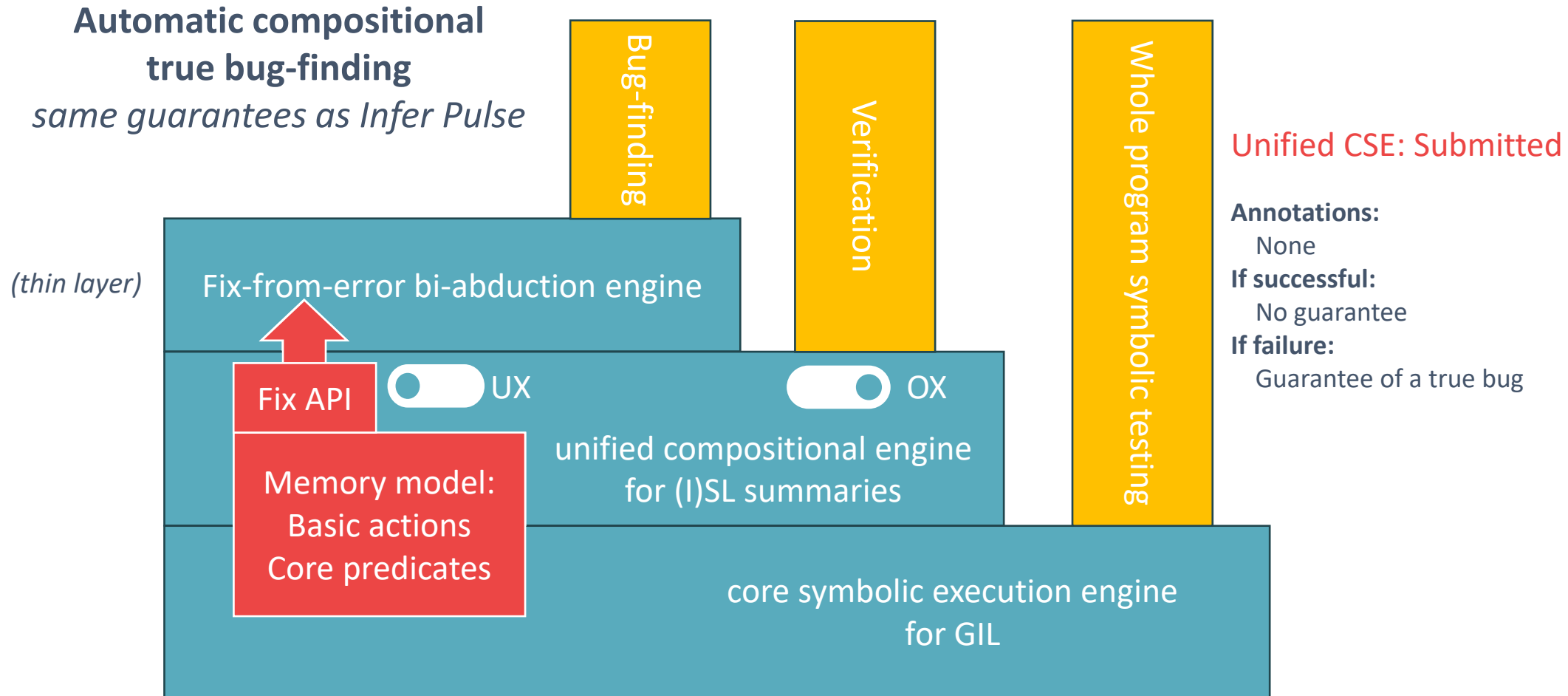
If failure:

Failing symbolic trace

Gillian: Unified Compositional Parametric Symbolic Execution



Gillian: Unified Compositional Parametric Symbolic Execution



Gillian Instantiations

WiSL (Gillian-While)	Simple block-offset model for teaching and experimentation Applied to data-structure algorithms
Gillian-JS	Extensible object memory model, JaVerT compiler Used for symbolic testing of Buckets-JS & verification of code from AWS Encryption SDK
Gillian-C	Block-offset memory model, CompCert and CBMC compilers Used for symbolic testing of Collections-C & verification of code from AWS Encryption SDK
Gillian-Rust	Step up from Gillian-C; partially laid-out heap, Iris ghost resources; Rust compiler + ours Used to verify parts of standard library (LinkedList & Vec)
Gillian-CHERI	Extension of Gillian-C memory model with support for CHERI capabilities

Gillian Student Lab



Gillian Verification Debugging

```

769 PFS/Gamma simplification:
770 With unification: No
771 PFS:
772 (w_el = { { #loc1, #offset1 } })
773 (w_er = { { #locr, #offsetr } })
774 (w_lor = #lloc)
775 (w_out = (offset1 < #offsetr))
776
777 Gamma:
778
779
780 Analysing list structure.
781 Analysing list structure.
782 PFS/Gamma simplification completed:
783
784 PFS:
785
786
787 Gamma:
788 (#offset1: Int)
789 (#offsetr: Int)
790
791 PFS/Gamma simplification:
792 With unification: No
793 PFS:
794 (w_el = { { #loc1, #offset1 } })
795 (w_er = { { #locr, #offsetr } })
796 (w_lor = #lloc)
797 (w_out = (offset1 < #offsetr))
798
799 Gamma:
800 (w_el: List)
801 (w_er: List)
802
803 Analysing list structure.
804 Analysing list structure.
805 PFS/Gamma simplification completed:
806
807 PFS:
808

```

```

3054 list(x, alpha)
3055
3056
3057
3058
3059
3060
3061
3062 Strategy 1: Examining list(x, alpha)
3063 Original values: [x, mu.]
3064 Extended values: [null, x]
3065 get_pred_with_vs. Strategy 1. Intersection of cardinal 1: [x]
3066 FOUND STH TO UNFOLD: list!!!!
3067
3068 Combine going to explode. PredPhase: list. Params: x, alpha. Args: x, alpha
3069
3070
3071
3072 Using unfold info, obtained subst:
3073 [ (alpha: #alpha), (x: x) ]
3074
3075 Going to produce 2 definitions with subst
3076 [ (alpha: #alpha), (x: x) ]
3077
3078 Produce assertion: types(alpha : List, #beta : List, #wsl_0 : Obj,
3079
3080
3081
3082
3083
3084
3085
3086 Produce simple assertion: types(alpha : List)
3087 With subst: [ (alpha: #alpha), (x: x) ]
3088
3089
3090
3091 STATE: SPEC VARS: #alpha, x
3092 STORE:
3093 [x: lvar #x]
3094

```

```

5090 TYPING ENVIRONMENT:
5091 (#alpha: List)
5092 (#x: List)
5093 (_lvar_5: List)
5094 (_lvar_6: Obj)
5095 (_lvar_7: Int)
5096
5097 PFS/Gamma simplification:
5098 With unification: No
5099 PFS:
5100 (x = { { _lvar_1, _lvar_7 } })
5101 (#alpha = l- ({ { _lvar_8 }, _lvar_5 })
5102 (_lvar_6 = _lvar_1)
5103 (01 <= (l-len #alpha))
5104 (01 <= (l-len #x))
5105 (01 <= (l-len _lvar_5))
5106
5107 Gamma:
5108 (#alpha: List)
5109 (#x: List)
5110 (_lvar_5: List)
5111 (_lvar_6: Obj)
5112 (_lvar_7: Int)
5113
5114 Analysing list structure.
5115 PFS/Gamma simplification completed:
5116
5117 PFS:
5118 (x = { { _lvar_1, _lvar_7 } })
5119 (#alpha = l- ({ { _lvar_8 }, _lvar_5 })
5120 (_lvar_6 = _lvar_1)
5121 (01 <= (l-len #alpha))
5122 (01 <= (l-len #x))
5123 (01 <= (l-len _lvar_5))
5124
5125 Gamma:
5126 (#alpha: List)
5127 (#x: List)
5128 (_lvar_5: List)
5129 (_lvar_6: Obj)

```

```

7783 Unify UP! There are 1 states left to consider.
7784 Substs:
7785 []
7786 [alpha]
7787 []
7788
7789 Unify assertion: (ret = (l-len #alpha)),
7790 Subst:
7791 [ (ret: 01), (#alpha: #alpha), (x: x) ]
7792 STATE:
7793 SPEC VARS: #alpha, x
7794 STORE:
7795 (ret: List 01)
7796
7797 MEMORY:
7798
7799 PURE FORMULAE:
7800 (x = null)
7801 (#alpha = { { } })
7802 (01 <= (l-len #alpha))
7803
7804 TYPING ENVIRONMENT:
7805 (#alpha: List)
7806 (#x: Null)
7807
7808 PREDS:
7809
7810 HANDS:
7811
7812 VARIANTS:
7813 llen,
7814
7815 Preparing entailment check:
7816 Existentials:
7817
7818 Left: (x = null)
7819 [ (#alpha = { { } })
7820 (01 <= (l-len #alpha))
7821 Right: (01 = (l-len #alpha))
7822 Gamma:

```



Old Gillian
(file log)

2019

Sacha, Petar

Logging
infrastructure

2020

Radu Lacraru

First debugger
(DAP-compliant)

2021

Matthew Ho

Visual
debugger!

2022

Nat Karmios

Source-level
debugging

2023

SSFT
lab

2025

TACAS
paper!

2026

A Gillian Taster

Link: <https://youtu.be/5TTBX4ecZkk>